# **MUTATIONS IN TIME:**

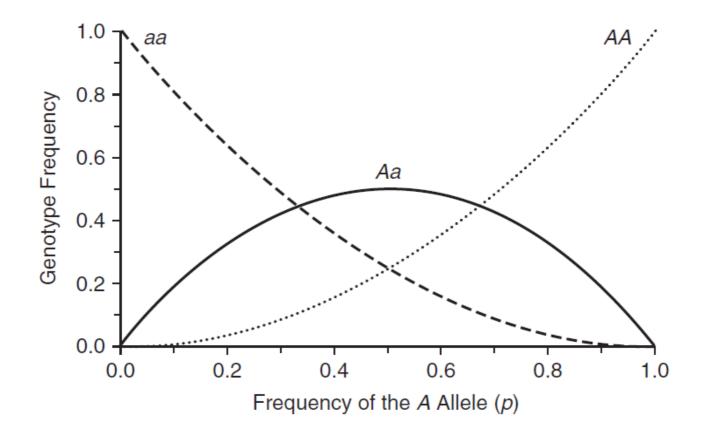
SOME BASICS OF POPULATION GENETICS

#### Lecture plan

- Hardy-Weinberg equilibrium
- Random genetic drift without mutations
- Effective population size
- Random genetic drift and mutations
- The coalescent theory
- Natural selection. Mutation-selection balance
- Random genetic drift, positive selection
- Selection coefficients, deleterious alleles
- Non-random mating, population subdivision, gene flow, admixture, adaptation

#### Hardy-Weinberg equilibrium (1908)

Generation 
$$N$$
:  $f_A = p$ ,  $f_a = q$ ,  $p + q = 1$   
Generation  $N + 1$ :  $F_{AA} = p^2$ ,  $F_{Aa} = 2pq$ ,  $F_{aa} = q^2$ 



Generation 
$$N$$
:  $f_A = p$ ,  $f_a = q$ ,  $p + q = 1$   
Generation  $N + 1$ :  $F_{AA} = p^2$ ,  $F_{Aa} = 2pq$ ,  $F_{aa} = q^2$ 

Implications:

1. The allele frequencies does not change:

$$p' = f'_A = F'_{AA} + F'_{Aa}/2 = p^2 + pq = p$$

*Exercise:* derive this

2. HWE frequencies are attained in one generation

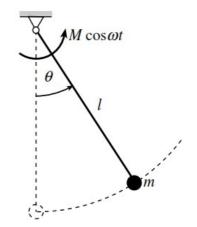
#### Assumptions:

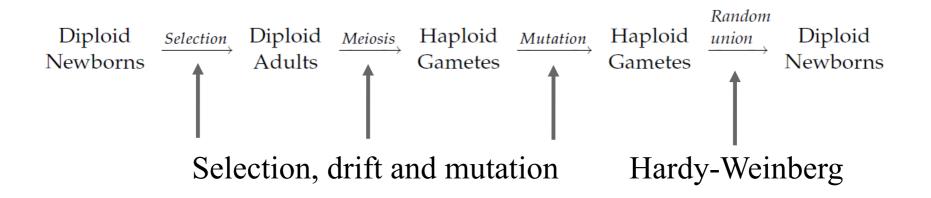
- Diploid species with sexual reproduction and random (not assortative) mating
- Same allele frequencies in males and females
- Non-overlapping generations
- Biallelic (autosomal) locus
- Population size is infinite
- No change in allele frequencies by migration, natural selection or mutation
- No genotyping errors

Does it still make sense with so many assumptions? Yes:

1. A baseline for more realistic models

2. The H-W model splits life history into two intervals: gametes  $\rightarrow$  zygotes and zygotes  $\rightarrow$  adults





#### Testing for HWE:

 $\chi^2 = \sum \frac{(O-E)^2}{E}$ 

df = n - k - 1, where n = 3 is the number of classes

and k = 1 is the number of independent parameters

Genotype	Observed Number ( <i>O</i> )	Expected Number (E)	(O-E)	$(O - E)^{2}$	$(O - E)^{2}/E$
AA	90	83.2	6.8	46.24	0.5558
Aa	28	41.6	-13.6	184.96	4.4462
аа	12	5.2	6.8	46.24	8.8923

After performing the calculations in this table, we get a chi-square ( $\chi^2$ ) statistic of

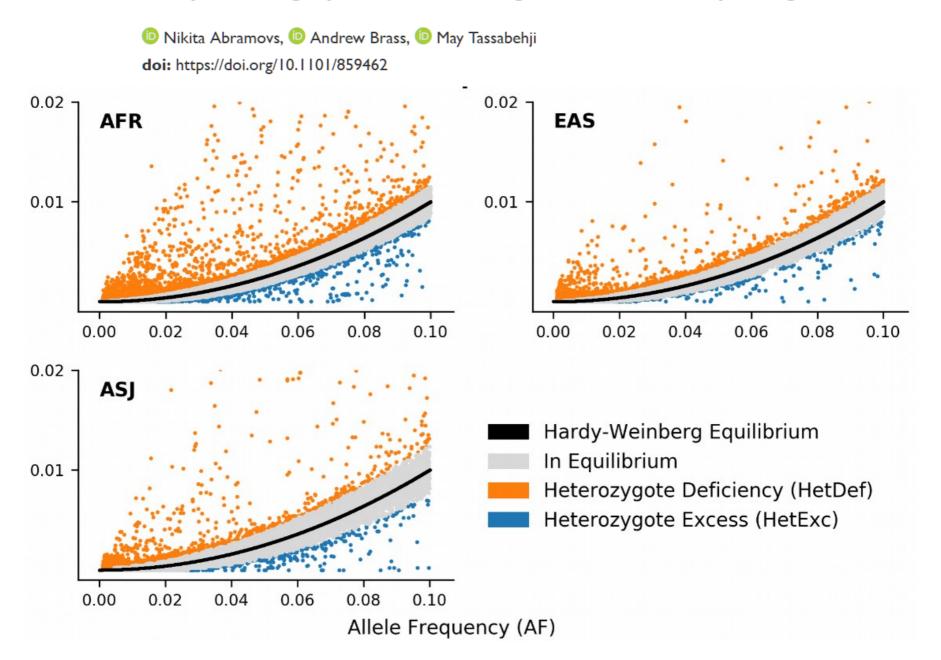
 $\chi^2 = 0.5558 + 4.4462 + 8.8923 = 13.8943$ 

This value is *much* larger than the critical value of 3.841, so we reject the hypothesis of Hardy–Weinberg equilibrium.

Exercise: do it yourself

Relethford – Human Population Genetics

#### Hardy-Weinberg Equilibrium in the Large Scale Genomic Sequencing Era



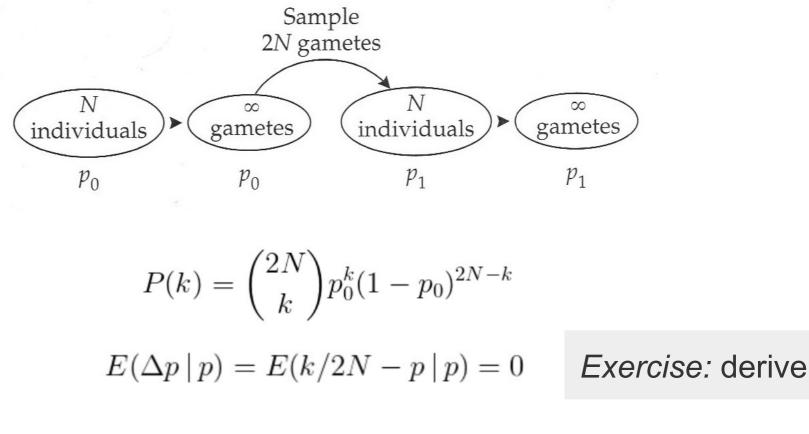
**gnomAD:** 137,842 predominantly healthy individuals from 7 major ethnic populations

# Random genetic drift (Wright-Fisher, 1930)

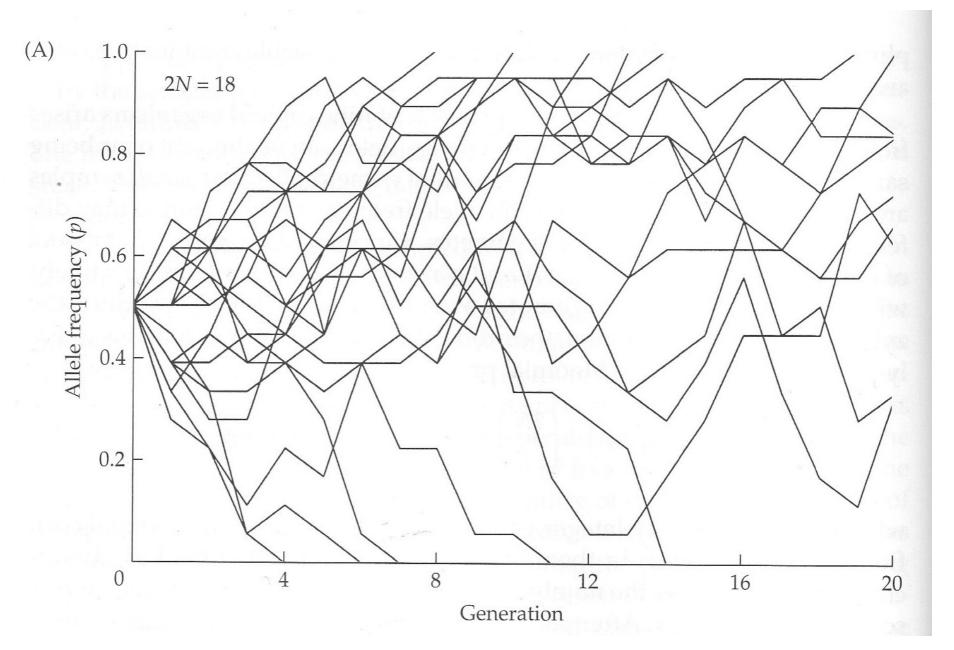
#### Assumptions:

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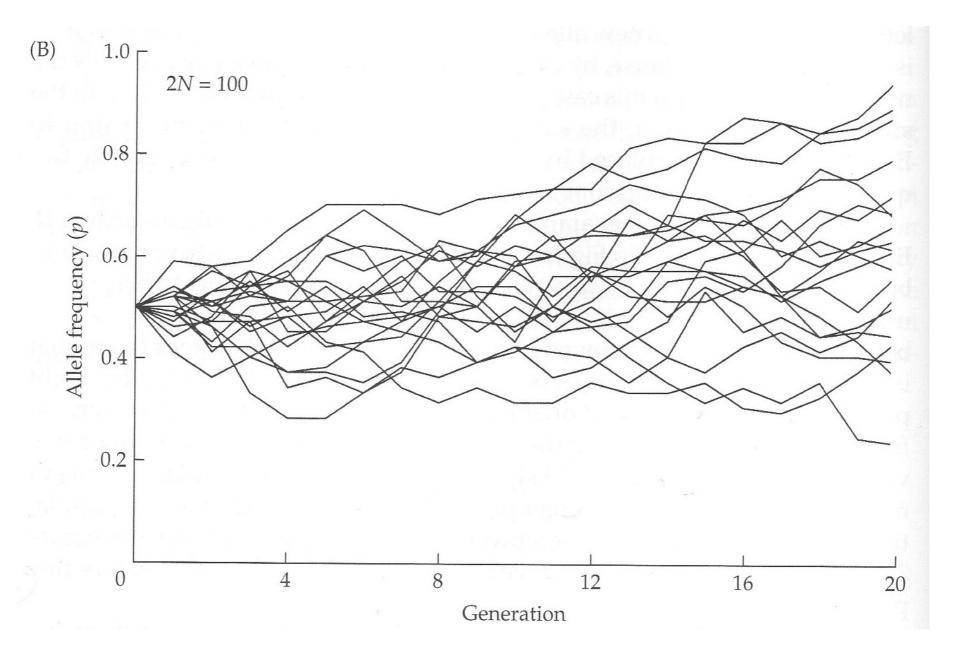
#### Finite population $\Rightarrow$ Sampling variation $\Rightarrow$ Allele frequency fluctuations $\Rightarrow$ Random genetic drift



 $Var(\Delta p | p) = Var(k/2N - p | p) = p(1 - p)/2N$ 



Hartl & Clark – *Principles of population genetics* 



Hartl & Clark – *Principles of population genetics* 

The endpoint is allele fixation or loss: P(F|p) = p

Mean time to fixation, if fixed:  $\overline{t_F}(p) = -4N\left(\frac{1-p}{p}\right)ln(1-p)$ 

Mean time to loss, if lost: 
$$\overline{t_L}(p) = -4N\left(\frac{p}{1-p}\right)ln(p)$$

Mean perstistence time:  $\overline{t}(p) = p\overline{t_F}(p) + (1-p)\overline{t_L}(p) =$ 

$$= -4N[(1-p)ln(1-p) + p \cdot ln(p)]$$

*Exercise:* at which *p* persistence time is maximal and what is it?

*Exercise:* estimate  $t_{F}(p)$  when  $p \rightarrow 0$ 

# Predicting the clinical impact of human mutation with deep neural networks

Laksshman Sundaram<sup>1,2,3,6</sup>, Hong Gao<sup>1,6</sup>, Samskruthi Reddy Padigepati<sup>1,3</sup>, Jeremy F. McRae<sup>1,4</sup>, Yanjun Li<sup>3</sup>, Jack A. Kosmicki<sup>1,4</sup>, Nondas Fritzilas<sup>1</sup>, Jörg Hakenberg<sup>1</sup>, Anindita Dutta<sup>1</sup>, John Shon<sup>1</sup>, Jinbo Xu<sup>5</sup>, Serafim Batzloglou<sup>1</sup>, Xiaolin Li<sup>3</sup> and Kyle Kai-How Farh<sup>1</sup>

Millions of human genomes and exomes have been sequenced, but their clinical applications remain limited due to the difficulty of distinguishing disease-causing mutations from benign genetic variation. Here we demonstrate that common missense variants in other primate species are largely clinically benign in human, enabling pathogenic mutations to be systematically identified by the process of elimination. Using hundreds of thousands of common variants from population sequencing of six non-human primate species, we train a deep neural network that identifies pathogenic mutations in rare disease patients with 88% accuracy and enables the discovery of 14 new candidate genes in intellectual disability at genome-wide significance. Cataloging common variation from additional primate species would improve interpretation for millions of variants of uncertain significance, further advancing the clinical utility of human genome sequencing.

Outside of modern human populations, chimpanzees comprise the next closest extant species, and share 99.4% amino acid sequence identity<sup>10</sup>. The near-identity of protein-coding sequence in humans and chimpanzees suggests that purifying selection operating on chimpanzee protein-coding variants might also model the consequences on fitness of human mutations that are identical-by-state. Because the mean time for neutral polymorphisms to persist in the ancestral human lineage ( $\sim 4N_e$  generations) is a fraction of the species' divergence time ( $\sim 6$  mya)<sup>11</sup>, naturally occurring chimpanzee variation explores mutational space that is largely non-overlapping except by chance, aside from rare instances of haplotypes maintained by balancing selection<sup>12,13</sup>. If polymorphisms that are identical-by-state similarly affect fitness in the two species, the presence of a variant at high allele frequencies in chimpanzee populations should indicate benign consequence in human, expanding the catalog of known variants whose benign consequence has been established by purifying selection.

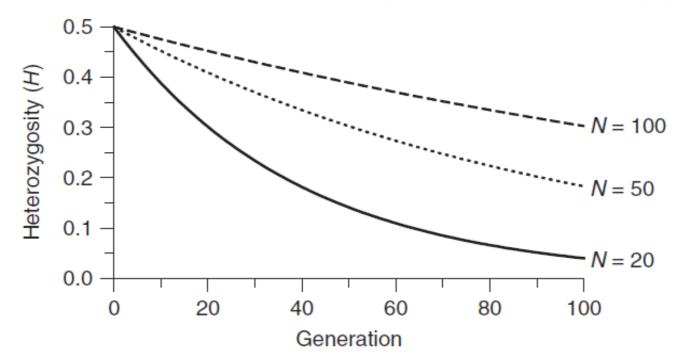
#### Random genetic drift and genetic variation

Heterozygosity: probability that an individuum is heterozygous at a locus: H = 2pq $H_{t+1} \simeq H_t - H_t/2N$ 

Heterozygosity decay due to drift:

$$H_t = H_0(1 - 1/2N)^t$$

Decay is slow:  $H_t = H_0/2$ :  $t \approx 2N \ln(2)$  for  $N \gg 1$ 



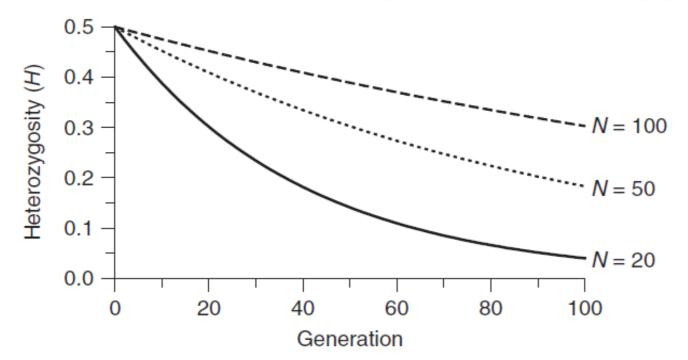
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### Effective population size

Effective population size of an actual population is the number of indivduals in a theoretically ideal population having the same magnitude of genetic drift as the actual population (Hartl & Clark, *Principles of population genetics*)

- Fluctuation in population size  $\frac{1}{N_e} = \frac{1}{t} \left( \frac{1}{N_0} + \frac{1}{N_1} + \dots + \frac{1}{N_{e-1}} \right)$
- Unequal sex ratio:  $N_e = \frac{4N_m N_f}{N_m + N_f}$  Exercise: bottleneck consequences for  $N_e$

 $N_e = \frac{N - 1}{(\sigma^2 / \xi) + (\xi - 1)}$ 

- Variance in offspring number:  $\sigma$ ,  $\xi$  – offspring mean and variance
- $N_e = Nd\left(1 + \frac{1}{4Nm}\right)$ • Subdivided population: d sub-populations of size N; m, migration

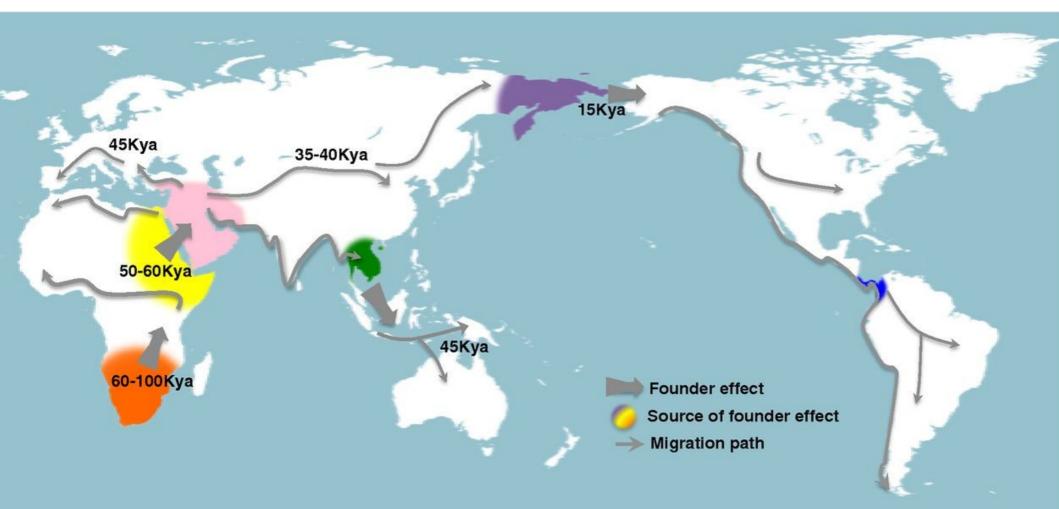
### Вопросы

В биаллельном локусе количество генотипов AA, Aa и aa составило 70, 20,10 (вариант 1) и 20, 70, 30 (вариант 2), соответственно. Можно ли сказать, что в данном локусе наблюдается равновесие Харди-Вайнберга? Рассчитайте и приведите ожидаемые частоты генотипов и значение критерия  $\chi^2$ . Для ответа на вопрос используйте критическое значение критерия 3.841



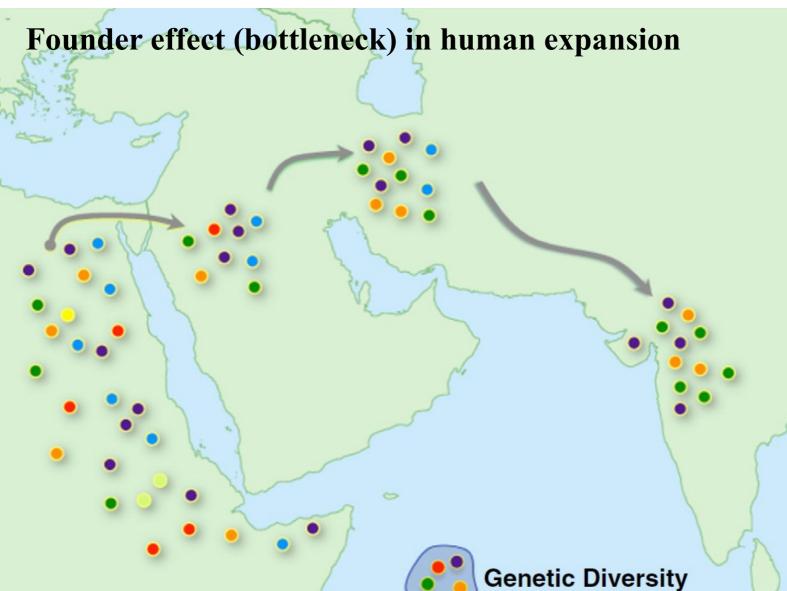
watch as we increase

# The great human expansion



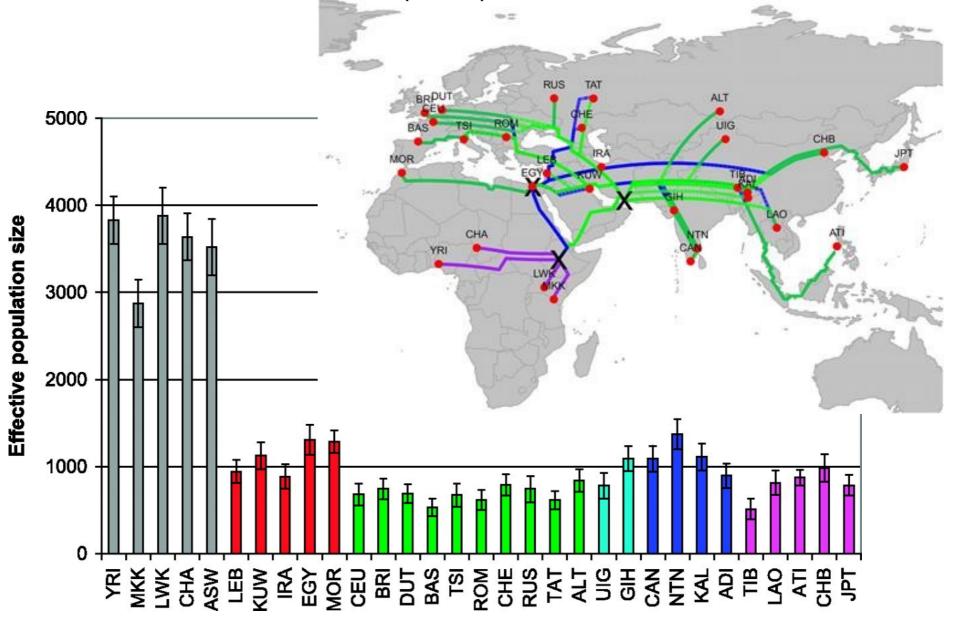
Resequencing studies have estimated the ancestral effective population size at 12,800 to 14,400, with a 5- to 10-fold bottleneck beginning approximately 65,000 to 50,000 y ago (although see ref. 15 for a bottleneck to only 450 individuals). Henn *et al* (2012) *PNAS* 

# The great human expansion



#### Henn et al (2012) PNAS

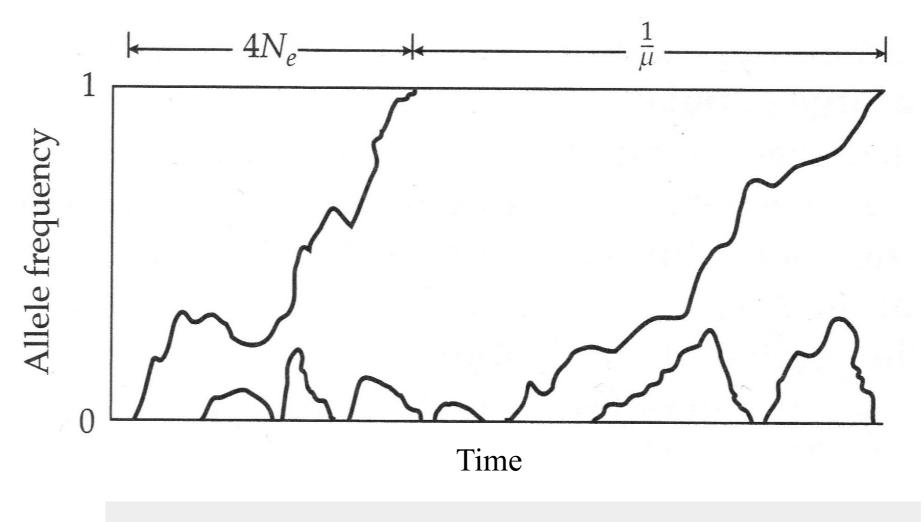
#### Recombination Gives a New Insight in the Effective Population Size and the History of the Old World Human Populations Mele *et al* (2011) *Mol Biol Evol*



**The neutral theory**: most mutations are selectively neutral with allele frequency determined by random genetic drift (Kimura 1968)

2N gametes  $\Rightarrow 2N\mu$  mutations in each generation, where  $\mu$  = mutations per gamete per generation Each mutation  $p_0 = 1/2N \Rightarrow P_{\text{Fix}} = 1/2N$ The steady-state rate at which neutral mutations are fixed in a population:  $k = 2N\mu P_{\text{Fix}} = \mu$ 

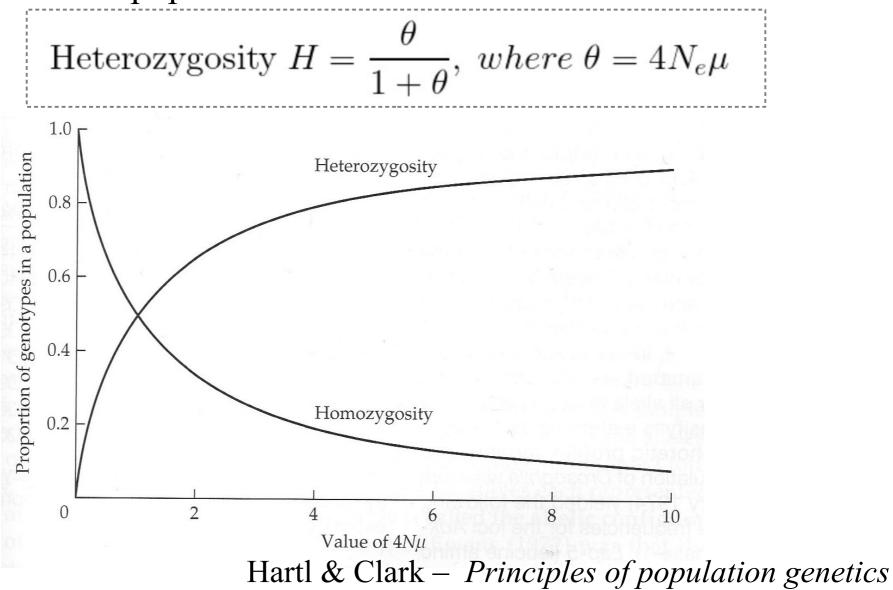
Mean time to fixation, if fixed:  $t_{\rm F}(p) = 4N_{\rm e}$  for  $p \approx 0$ 



*Exercise:* estimate fixation time for a new neutral allele

Hartl & Clark – *Principles of population genetics* 

The infinite-alleles model: each mutation creates a new allele in the population



**The infinite-alleles model:** each mutation creates a new allele in the population

Heterozygosity 
$$H = \frac{\theta}{1+\theta}$$
, where  $\theta = 4N_e\mu$ 

 $N_{\rm e}$ : effective population size, ~10,000  $\mu$ : mutation rate per site per generation, ~1.2×10<sup>-8</sup>

$$\theta = 4 \times 10^4 \times 1.2 \times 10^{-8} \approx 5 \times 10^{-4}$$

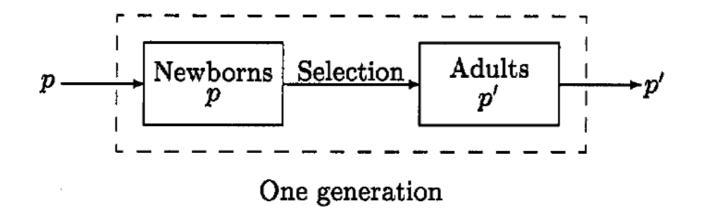
$$\theta << 1 \Longrightarrow H \approx \theta = 1/2000$$

The neutral (Motoo Kimura) and nearly neutral (Tomoko Ohta) theory of molecular evolution (1960-70):

- Random genetic drift of [nearly] neutral alleles is the source of polymorphism, not balancing selection.
- Most substitutions (fixations) are due to random drift of neutral mutants, not advantageous mutations
- Missing substitutions are then evolutionary forbidden

A CACAAAAAG T G G AAAA C <mark>A G T T AA T G A C C AG C C AC</mark> G G C G T C C C T G C T G T G A G C T C T G G C C G C T G C C T T C C A G A1\_Human/1-395 A CACAAAAG T G G AAAA C <mark>A G T T AA T G</mark> A <mark>C C A G C C A C</mark> G G C A <mark>T C C C T G</mark> C T G T G A G C T C C G C C G C T G C C T T C C A G A1 Macague/1-452 A CACAAAAG T G G AAAG C AG T T AA T G A C C AG C C AC AG T A T C C C T G C T G AG C T C T G G C C AC T G C C T T C C AC A1 Mouse lemun/1-402 ACACAAAAGTGGAAAACAGTTAATGACCAGCCACAGCGTCTGCTGTGA--GCTTCGGCCAGTGCC-TCCAC A1 Squimel/1-371 A1 Mouse/1-320 AAACAAAAGTGGAAAGC<mark>AGTTAATG</mark>ACCAGCCACAGCGGCTTTGCTACAAGCTCTGGCCGCTGCCCCCAAC A1\_Rabbit/1-418 A C A C A A A A G T G G A A A A C A G T T A A T G A C C A G C C A G C G C T C C T G C T G C T G C T G C T G C T C C A G A A1 Cat/1-399 A C A C C A A A G T G G A A A A C A G T T A A T G A C C A G C C A C A G C G T C C C G T G A G T T C C G G C C A C T G C C C C C A C C A1 Armadillo/1-400 A1\_Tasmanian\_devil/1-95 · · ..... TTAATGACCAGCCACAGTGTCCCTGCCCAGCGCTACCTCTGCTCCCCCCAC1 AAACAAAAGTGGAAAGCAGTTAATGACCAGCCACGGTGTCCTTGCCCAGTGCTGCCTCTGCTCCCCCCCAC1 A1\_Opossum/1-424 CTCCTGTTTTATCTTCCAGTTAATGACCAGCCACAGTGTCCCTGCAGTGTGCTGTTGCCACTGCCCCTGT( A1\_Platypus/1-137 CCCCGGCCCGGAGTTAATGCCCAGCCATAACGTCCTTGTTGTGTACTGCTGCTGCTGCCGCACAAAGC A1\_Chicken/1-206 - TTAATGCCTGGCCACAACAT - CTGTACTGTACTGCTGCTGCTGCTACAAAG4 A1 Flycatcher/1-76 CCATCAAACTGGCGAGG<mark>AGTTGATGACCAGCCAC</mark>AGTAG<mark>CTCTGCTGTGTGCT</mark>GTTT<mark>C</mark>CATCCAAGGTGC1 A1\_Anole\_lizard/1-294 AGCCAAGTGGGGAAAAA<mark>AGTTAATG</mark>T<mark>CC</mark>GA<mark>C</mark>AATA<mark>TC</mark>CC**TG**CTGCAT<mark>G</mark>AGTGGAGCTGCTACTGGGA/ A1\_Coelacanth/1-296

**Natural selection** is the differential survival and reproduction of individuals resulting from differences in phenotype. Natural selection changes allele frequencies:



**Fitness** is an individual's ability to propagate its alleles ≈ viability [+fertility+developmental time+mating, ...]

**Deleterious** alleles reduce fitness (*≠* pathogenic, damaging)

Gillespie – Population genetics. A concise guide

#### TABLE 5.2 Diploid Selection for Survivorship (Viability)

		Genotype		Total	
Generation $t - 1$	AA	Aa	аа	- ×	
Frequency before selection	$p^2$	2pq	$q^2$	$1 = p^2 + 2pq + q^2$	
Relative fitness (viability)	$w_{11}$	$w_{12}$	$w_{22}$		
After selection	$p^2 w_{11}$	$2pqw_{12}$	$q^2 w_{22}$	$\overline{w} = p^2 w_{11} + 2pqw_{12} + q^2 w_{22}$	
Normalized	$\frac{p^2 w_{11}}{\overline{w}}$	$\frac{2pqw_{12}}{\overline{w}}$	$\frac{q^2 w_{22}}{\overline{w}}$	$w_{11} > 0, w_{12} \ge 0, w_{22} \ge 0$	
Generation t		$p' = \frac{p^2 w_{11} + pq}{\overline{w}}$ $q' = \frac{pq w_{12} + q^2}{\overline{w}}$			
$\Delta p$ =	$= \frac{pq[p(w)]}{pq[p(w)]}$	$(w_{11} - w_{12}) - \bar{w}$	$+q(w_{12})$	$-w_{22})]$	
Exercise: derive	Hartl	& Clark –	Princip	les of population gene	

Hartl & Clark – *Principles of population genetics* 

Genotype Viability (fitness) Relative fitness

 $A_1A_1$   $A_1A_2$   $A_2A_2$  $W_{11}$   $W_{12}$   $W_{22}$ 1  $W_{12}/W_{11} W_{22}/W_{11}$ 

Genotype $A_1A_1$  $A_1A_2$  $A_2A_2$ Viability (fitness) $w_{11}$  $w_{12}$  $w_{22}$ Relative fitness1 $w_{12}/w_{11}$  $w_{22}/w_{11}$ Relative fitness11-hs1-swhere  $0 \le s \le 1$  is the selection coefficient,h is the heterozygous effect and measures dominance

h = 0	$A_1$ dominant, $A_2$ recessive // 1, 1, 1-s				
h = 1	$A_1$ recessive, $A_2$ dominant // 1, 1-s, 1-s				
$0 \le h \le 1$	incomplete dominance				
$h = \frac{1}{2}$	additivity	// 1, 1- <i>s</i> /2, 1- <i>s</i>			
$h \leq 0$	overdominance				
h > 1	underdominance	<i>Exercise: h&lt;</i> 0, <i>h&gt;</i> 1			

$$\Delta p = \frac{pq[p(w_{11} - w_{12}) + q(w_{12} - w_{22})]}{\bar{w}}$$

Switch to relative fitness:  $w_{12}/w_{11} = 1 - hs$ ,  $w_{22}/w_{11} = 1 - s$ 

$$\begin{split} \Delta p &= \frac{pqs[ph+q(1-h)]}{\tilde{w}} \\ \tilde{w} &= 1-2pqhs-q^2s \end{split}$$

Exercise: derive

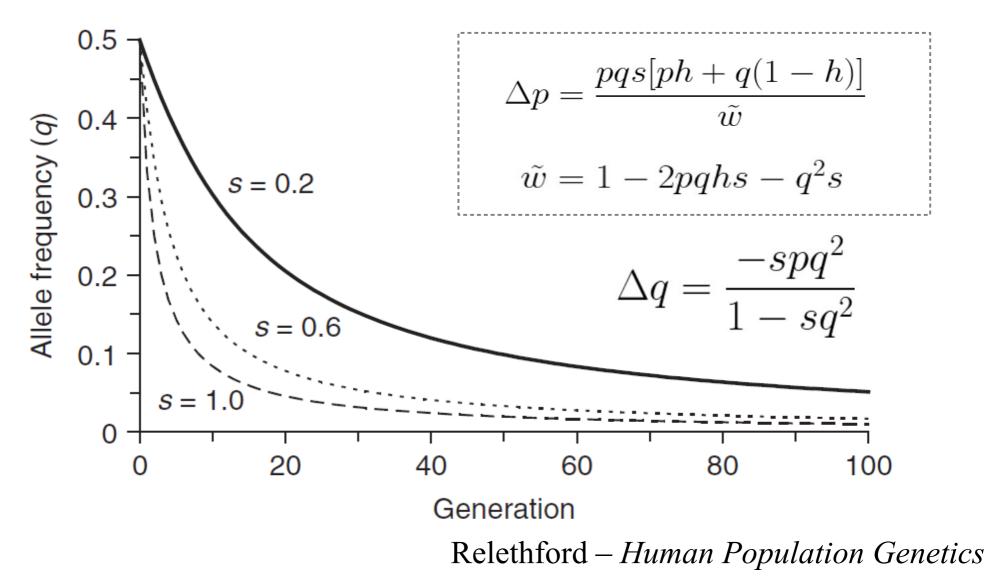
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**1. Directional (positive, negative, purifying) selection** Recessive allele:  $w_{11}=1$ ,  $w_{12}=1$ ,  $w_{22}=1-s$  //  $w_{12}=1$ Dominant allele:  $w_{11}=1$ ,  $w_{12}=1-s$ ,  $w_{22}=1-s$  //  $w_{12}=w_{22}$ Incomplete dominance:  $w_{11}=1$ ,  $w_{12}=1-hs$ ,  $w_{22}=1-s$ , 0 < h < 1//  $w_{11} > w_{12} > w_{22}$  **2. Balancing selection** Overdominance:  $w_{11}=1$ ,  $w_{12}=1-hs$ ,  $w_{22}=1-s$ , h < 0 //  $w_{12} > w_{11,22}$ 

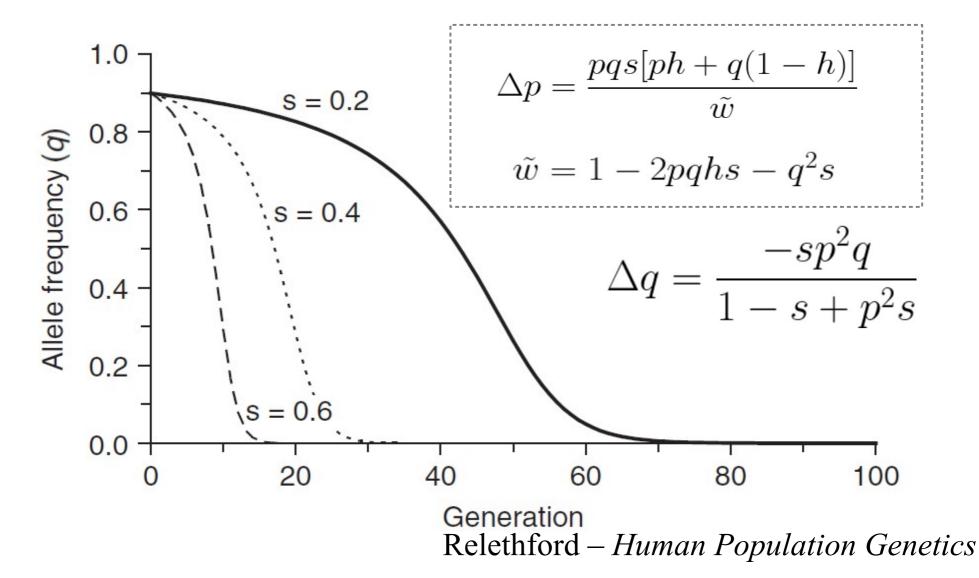
#### **3. Disruptive selection** Underdominance: $w_{11}=1$ , $w_{12}=1-hs$ , $w_{22}=1-s$ , h > 1

*Exercise:* valid range for *h* ?

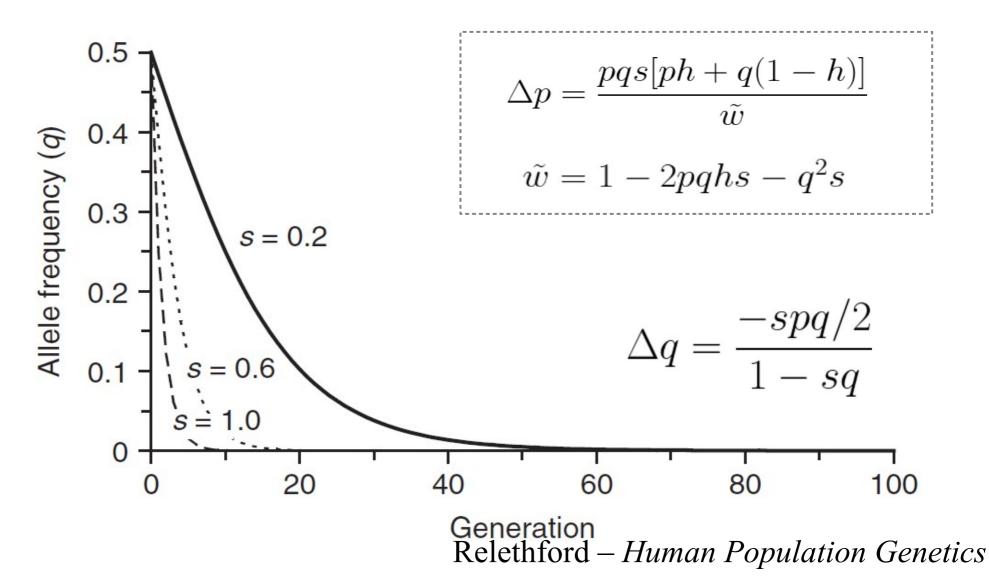
Directional selection against a recessive allele:  $w_{11} = w_{12} = 1, \ w_{22} = 1 - s$ 



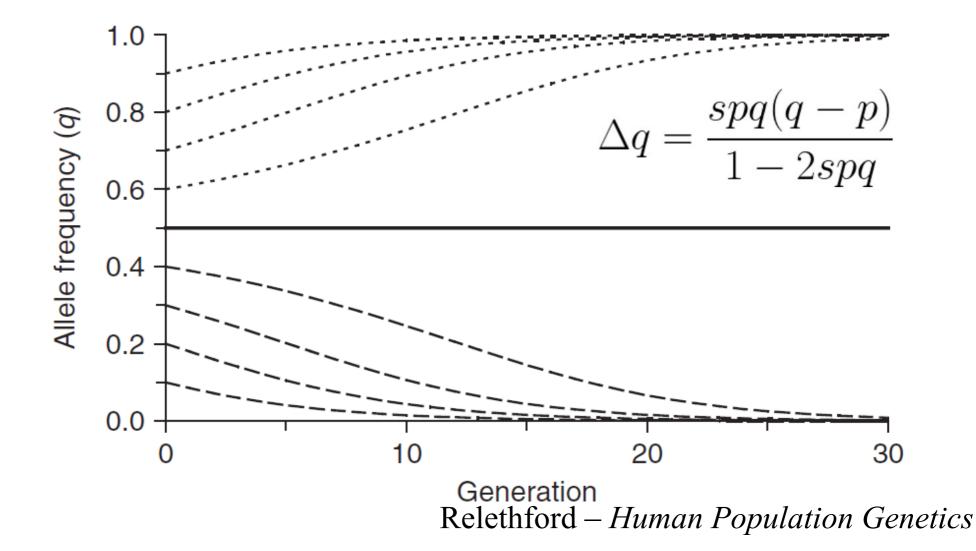
Directional selection against a dominant allele:  $w_{11} = 1, \ w_{12} = w_{22} = 1 - s$ 



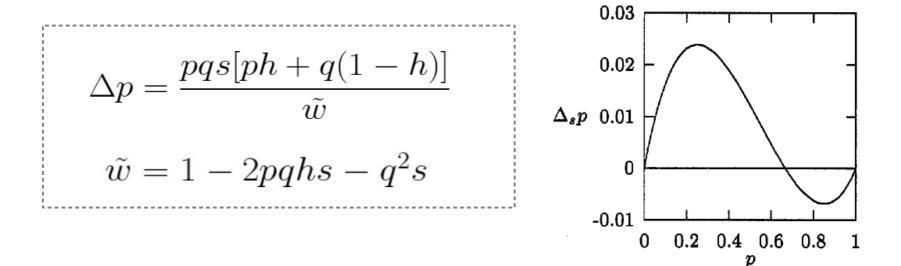
Directional selection against a codominant additive allele:  $w_{11} = 1$ ,  $w_{12} = 1 - s/2$ ,  $w_{22} = 1 - s/2$  incomplete dominance



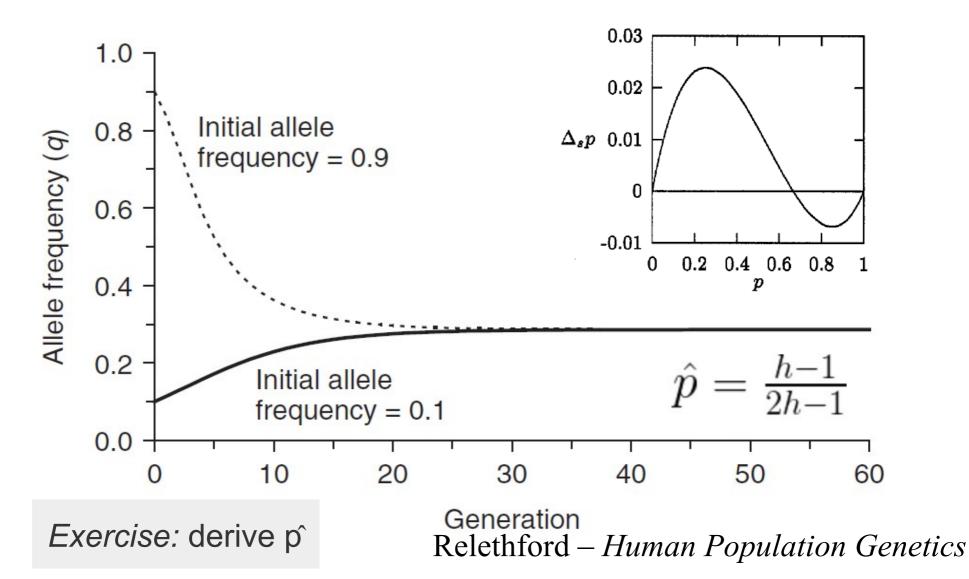
Disruptive selection against a heterozygote:  $w_{11} = 1, w_{12} = 1 - s, w_{22} = 1$  // underdominance



Balancing selection for a heterozygote:  $w_{11}=1, w_{12}=1-hs, w_{22}=1-s, h < 0$  // overdominance



#### Balancing selection for a heterozygote: $w_{11}=1, w_{12}=1-hs, w_{22}=1-s, h < 0$ // overdominance



### Balancing selection: the case of CF

#### **BOX 3.7 SELECTION IN FAVOR OF HETEROZYGOTES FOR CYSTIC FIBROSIS**

For CF, the disease frequency in Denmark is about one in 2000 births.

Phenotypes:	Unaffected		Affected
Genotypes:	AA	Aa	aa
Frequencies:	p <sup>2</sup>	2pq	$q^2 = 1/2000$

 $q^2$  is 5 × 10<sup>-4</sup>; therefore q = 0.022 and p = 1 - q = 0.978.

 $p/q = 0.978/0.022 = 43.72 = s_2/s_1.$ 

If  $s_2 = 1$  (affected homozygotes never reproduce),  $s_1 = 0.023$ .

The present CF gene frequency will be maintained, even without fresh mutations, if Aa heterozygotes have on average 2.3% more surviving children than AA homozygotes.

*Exercise:* express heterozygous advantage *h* as a function of  $p^{\uparrow}$ , verify estimate above



Strachan, Read – Human Molecular Genetics

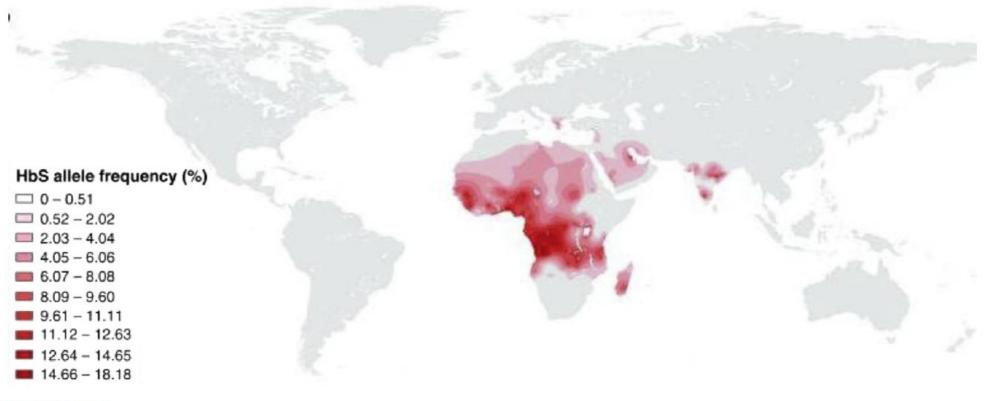
#### Balancing selection: the case of B-hemoglobin

The most thoroughly studied example of overdominance is the sickle-cell hemoglobin polymorphism found in many human populations in Africa. Hemoglobin, the oxygen-carrying red protein found in red blood cells, is a tetramer composed of two alpha chains and two beta chains. In native West and Central African populations, the S allele of beta hemoglobin reaches a frequency as high as 0.3 in some areas. The more common A allele is found at very high frequency in most other areas of the world. The two alleles differ only in that the S allele has a glutamic acid at its sixth amino position while the A allele has a valine. The glutamic acid causes the hemoglobin to form crystal aggregates under low partial pressures of oxygen, as occur, for example, in the capillaries. As a result, SS homozygotes suffer from sickle-cell anemia, a disease that is often fatal.

The S allele could not have reached a frequency of 0.3 unless AS heterozygotes are more fit than AA homozygotes. This is precisely the case in regions where malaria is endemic, for there the heterozygotes are somewhat resistant to severe forms of malaria. The resistance is due to the sickling phenomena, which makes red blood cells less suitable for *Plasmodium falciparum*. In an old study from 1961, it was shown that the viability of AS relative to AA is 1.176 in regions with malaria. Assuming that the fitness of SS is zero (s = 1), h = -0.176. Plugging this into Equation 3.4 gives  $\hat{p} = 0.87$  or  $\hat{q} = 0.13$  for the S allele, which is nestled right in the middle of allele frequencies in regions with endemic malaria.



### Balancing selection: the case of B-hemoglobin



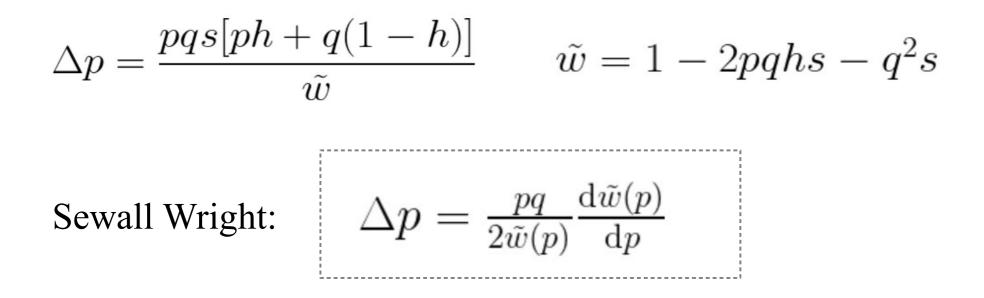
#### FIGURE 14.2

The global distribution of the sickle-cell allele.

From Piel, F.B., Patil, A.P., Howes, R.E., Nyangiri, O.A., Gething, P.W., Williams, T.N., et al., 2010. Global distribution of the sickle cell gene and geographical confirmation of the malaria hypothesis. Nature Communications 1, 104–104.



Templeton - Human Population Genetics and Genomics (2019)



What happens to  $\widetilde{w}(p)$  ?

"Natural selection always increases the mean fitness and does so at a rate that is proportional to the genetic variation"

#### Mutation-selection balance

- Many new alleles are deleterious and incompletely dominant.
- They enter the population by mutation and are removed by negative selection.  $A_1(p \approx 1) \xrightarrow{\mu} A_2(q \approx 0)$
- Balance: the rate of introduction of mutations equals rate of loss due to selection

$$\Delta_{mut} p = -\mu p \approx -\mu$$
$$\Delta_{sel} p = \frac{pqs[ph+q(1-h)]}{1-2pqhs-q^2s} \approx qhs$$
$$uut p + \Delta_{sel} p = 0 \qquad \qquad \hat{q} \approx \frac{\mu}{hs}$$

#### Mutation-selection balance

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for a recessive allele

#### Random drift and advantageous allele

Selection in finite population is very weak for *de novo* alleles: New allele:  $\Delta p \approx (1+s)p - p = sp = s/2N << 1/2N$  (drift), unless s  $\approx 1$ 

$$P_F(p) = \frac{1 - e^{-2Nsp}}{1 - e^{-2Ns}}, \text{ if } h = 1/2$$

$$P_F(1/2N) = \frac{1 - e^{-s}}{1 - e^{-2Ns}} \qquad P_F \approx s \text{ if } s \approx 0 \text{ and } 2Ns >> 1$$

#### Random drift and advantageous allele

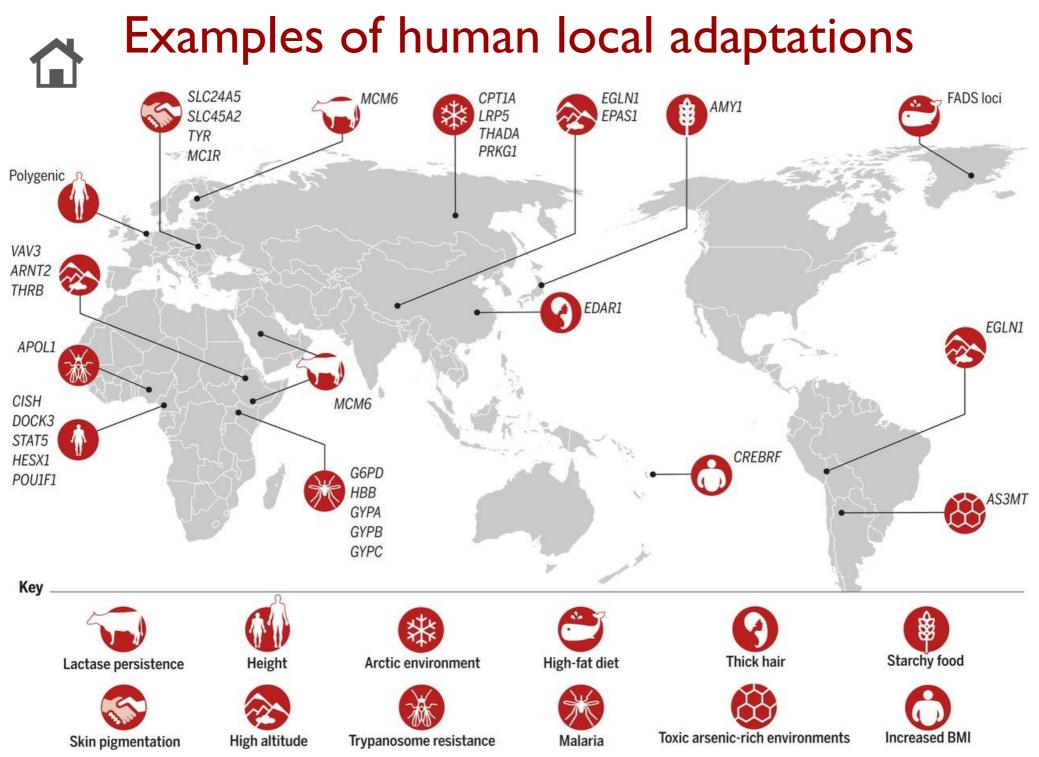
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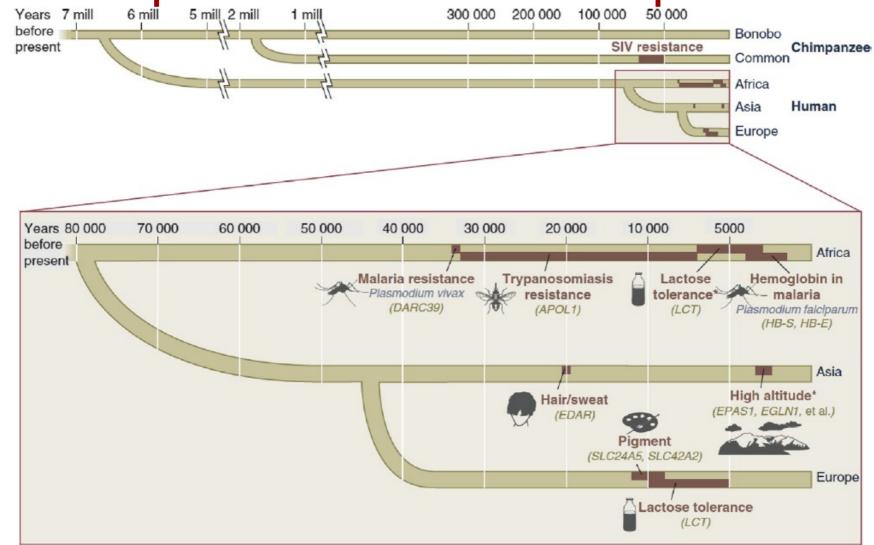
- Most advantageous alleles are lost.
- Adaptive evolution is random

*Exercise:* 
$$P_{\rm F}$$
 for s,  $2Ns \approx 0$ 



Fan (2016)

### Examples of human local adaptations



#### FIGURE 14.4

A portrayal of human evolution in a combined species and intraspecific population phylogenetic tree. Various points on the human "branches" indicate the estimated times at which various positively selected human adaptations arose.

From Vitti, J.J., Cho, M.K., Tishkoff, S.A., Sabeti, P.C., 2012. Human evolutionary genomics: ethical and interpretive issues.

Trends in Genetics 28, 137–145. Templeton - Human Population Genetics and Genomics (2019)

#### Random drift and deleterious allele

Can a deleterious allele fix in a finite population?

$$\begin{split} P_F(q) &= 1 - P_F(1-q) = \frac{e^{2Nsq} - 1}{e^{2Ns} - 1} \\ P_F(1/2N) \approx \frac{s}{e^{2Ns} - 1} \quad \mathbf{P_F} \approx \mathbf{0} \text{ if } \mathbf{2Ns} >> 1 \end{split}$$

Gillespie – Population genetics. A concise guide

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#### Random drift and deleterious allele

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Fixation rate for deleterious alleles:

$$k = 2N\mu P_F(1/2N) = \frac{2N\mu s}{e^{2Ns} - 1} \qquad \text{Exercise: } P_{\rm F} \text{ for } s \to 0$$
  
Exercise: k for s  $\to 0$ ?

#### Mildly deleterious vs neutral mutations

Mutations can be placed in three main categories:

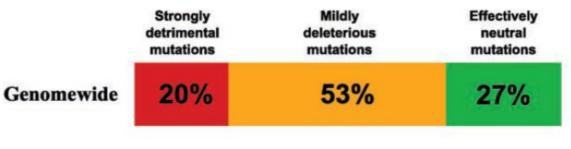
- those that are selected (either positively or negatively);
- those that are neutral (i.e. have no effect on fitness) and
- those that have low selection coefficients, and thus behave as neutral in small populations (where the effects of drift dominate) or are selected in large populations, where the deterministic effects of selection prevail

Meyer, Diogo; and, Harris, Eugene E (March 2008) Selection Operating on Protein-coding Genes in the Human Genome. In: Encyclopedia of Life Sciences (ELS). John Wiley & Sons, Ltd: Chichester. DOI: 10.1002/9780470015902.a0020791

### Mildly deleterious vs neutral mutations

#### Most Rare Missense Alleles Are Deleterious in Humans: Implications for Complex Disease and Association Studies

Gregory V. Kryukov, Len A. Pennacchio, and Shamil R. Sunyaev The American Journal of Human Genetics Volume 80 April 2007

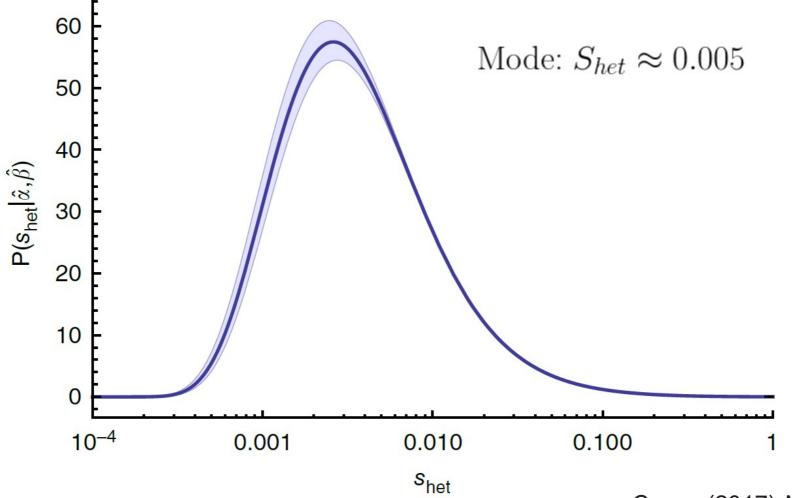


0.003 ... 0.001

We combined analysis of mutations causing human Mendelian diseases, of human-chimpanzee divergence, and of systematic data on human genetic variation and ... estimated that >50% of *de novo* missense mutations in an average human gene and 70% of missense SNPs detected only once among 1,500 chromosomes are mildly deleterious. Such **mildly deleterious mutations are associated with selection coefficients within a surprisingly narrow range of 0.001–0.003** Kryukov (2007) Am J Hum Genet

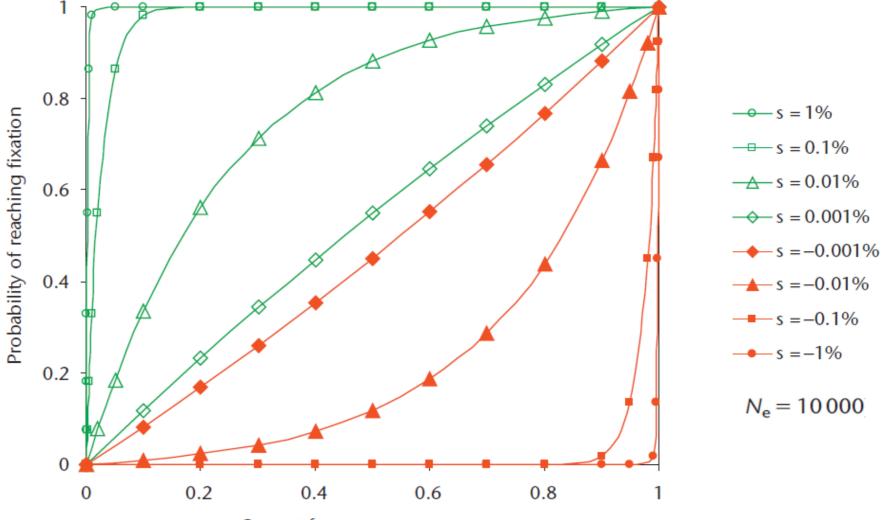
# Estimating the selective effects of heterozygous protein-truncating variants from human exome data

Christopher A Cassa<sup>1,2,9</sup>, Donate Weghorn<sup>1,9</sup>, Daniel J Balick<sup>1,9</sup>, Daniel M Jordan<sup>3,9</sup>, David Nusinow<sup>1</sup>, Kaitlin E Samocha<sup>4,5</sup>, Anne O'Donnell-Luria<sup>4,6</sup>, Daniel G MacArthur<sup>2,4</sup>, Mark J Daly<sup>2,4</sup>, David R Beier<sup>7,8</sup> & Shamil R Sunyaev<sup>1,2</sup> VOLUME 49 | NUMBER 5 | MAY 2017 NATURE GENETICS



Cassa (2017) Nat Genet

#### Fixation probabilities for all alleles



Current frequency

Thomas, Paul D (July 2008) Single Nucleotide Polymorphisms in Human Disease and Evolution: Phylogenies and Genealogies. In: Encyclopedia of Life Sciences (ELS). John Wiley & Sons, Ltd: Chichester. DOI: 10.1002/9780470015902.a0020763

## Summary

What changes allele/genotype frequencies?

- Mutation: introduction of new alleles into a population
- Genetic drift: sampling variation of transmitted alleles
- Selection: different probabilities of survival/reproduction depending on genotypes
- Gene flow: movement of alleles due to migration
- Non-random mating of individuals in a population

# Summary

- Hardy-Weinberg equilibrium describes how zygotes originate from gametes
- Random genetic drift drives alleles to loss or fixation and reduces heterozygosity
- Neutral theory postulates that most inter- and intra-species changes are due to negative selection and random drift
- A coalescent is the lineage of alleles in a sample traced backward in time to their common ancestor allele
- Natural selection changes allele frequencies. It always increases the mean fitness and does so at a rate that is proportional to the genetic variation
- Most new alleles are deleterious and incompletely dominant. They appear by mutation and are subject to negative selection (mutation-selection balance).
- In a finite population, a new advantageous mutation is usually lost because of random drift. On the other hand, a deleterious allele can fix.

### Further reading

- Meyer, D., Harris, E. (2008) Selection Operating on Protein-coding Genes in the Human Genome. In: *Encyclopedia of Life Sciences* (ELS). doi:10.1002/9780470015902.a0020791
- Nei, M., Suzuki, Y., and Nozawa, M. (2010). The neutral theory of molecular evolution in the genomic era. *Annu Rev Genomics Hum Genet* 11, 265–289
- Hurst, L.D. (2009). Genetics and the understanding of selection. *Nature Reviews Genetics* 10, 83–93.
- Fan, S., Hansen, M.E.B., Lo, Y., and Tishkoff, S.A. (2016). Going global by adapting local: A review of recent human adaptation. *Science* 354, 54–59.
- John H. Gillespie Population Genetics. A concise guide
- John H. Relethford Human population genetics